

## FOAM FINNED DOWN FLOW TYPE AUTOMOTIVE RADIATOR RATING AND SIZING

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### ABSTRACT

Radiator is ubiquitous cooling module of engine cooling system in automobiles. Recent advancement in engine for power forced engine cooling system is to improve its efficiency and also reduce fuel consumption along with control of engine emission to meet environmental pollution norms. It prompted investigation of alternative materials for radiators to improve its efficiency. Carbon foam was found to be one of the implementable alternative materials for fins in radiators core by considering primary factors which influence radiator performance. The most common radiator design glitches are rating and sizing. In this article,  $\epsilon$ -NTU method is described to estimate heat transfer calculations for foam finned down flow type radiator. An application in Microsoft Excel™ is developed to assist in the calculations and analysis of radiator parameters and heat rejection for predefined size.

**KEYWORDS:** Down flow radiator, Carbon foam, Heat transfer, Thermal conductivity (TC)

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### NOMENCLATURE

Symbols	Abbreviations		
$C_w$	Core width	$C_{p_c}$	Specific heat of coolant
$C_L$	Core length	$k_c$	TC of coolant
$C_d$	Core depth	$Nu_c$	Nusselt number of coolant
$C_v$	Core volume	$f_D$	Darcy friction factor
$T_w$	Tube width	$h_c$	Heat transfer coefficient of coolant
$T_h$	Tube Height	$D_{ha}$	Hydraulic diameter of air
$T_d$	Tube depth	$A_{ra}$	Free flow area of air
$T_t$	Tube thickness	$A_a$	Total heat transfer area
$F_h$	Fin Height	$Re_a$	Reynolds number for air
$F_d$	Fin Width	$V_a$	Velocity of air
$F_t$	Fin thickness	$S_a$	Kinematic viscosity of air
$F_p$	Fin pitch	$\mu_a$	Dynamic viscosity of air
$N_r$	Number of rows for tube/fin	$\rho_a$	Density of air
$D_{tr}$	Distance between the tube rows	$Pr_a$	Prandtl number of air
$N_{tube}$	Number of Tubes	$C_{p_a}$	Specific heat of air
$N_{fin}$	Number of columns of Fins	$k_a$	TC of air
$D_{hc}$	Hydraulic diameter of coolant	$Nu_a$	Nusselt number of air
$A_{it}$	Inside cross-section area of tube	$h_a$	Heat transfer coefficient of air
$A_{isat}$	Total inside surface area of the tube	$C_a$	Heat capacity rate for air
$P_{it}$	Inside perimeter of tube	$A_{osaf}$	Total outer surface area of the fin

$Re_c$	Reynolds number for coolant	$M_a$	Mass flow rate of air
$V_c$	Velocity of coolant	$C_c$	Heat capacity rate for coolant
$W_c$	Volume flow rate of coolant	$C_r$	Heat capacity rate ratio
$M_c$	Mass flow rate of coolant	$\eta_{fin}$	Fin efficiency
$\rho_c$	Density of coolant	$m_f$	Coefficient for calculating efficiency of fin
$\mu_c$	Dynamic viscosity of coolant	$k_f$	TC of fin material
$S_c$	Kinematic viscosity of coolant	$F_{cl}$	Corrected fin length
$Pr_c$	Prandtl number of coolant	$\eta_o$	Overall surface efficiency
$A_b$	Base surface area	$N_{fin/tube}$	Number of fins per tube
$A_{fin, base}$	Total fin/base surface area of a single tube	$U$	Overall heat transfer coefficient
$R$	Overall thermal resistance	$NTU$	Number of transfer units
$A_c$	Total heat transfer area of coolant	$C_{min}$	Minimum heat capacity
$k_t$	TC of tube material	$C_{max}$	Maximum heat capacity
$\eta_{tube}$	Tube efficiency	$\varepsilon$	Effectiveness
$m_t$	Coefficient for calculating efficiency of tube	$Q_{max}$	Maximum heat transfer rate
$T_{cl}$	Corrected tube length	$Q_{pred}$	Predicted heat transfer rate
$A_f$	Single fin surface area	$T_{ic}$	Inlet coolant temperature
$P_f$	Perimeter of fin	$T_{oc}$	Outlet coolant temperature
$P_{tube}$	Perimeter of Tube	$T_{ia}$	Inlet air temperature
$F_p$	Fin density	$T_{oa}$	Outlet air temperature
$R_A$	Fin surface roughness due to the exposed pores	$A_{tpb}$	Total interior heat transfer surface available in interconnected pore channel
$Re_d$	Pore level Reynold number	$Re_L$	Reynolds number in fin channel
$D_E$	Equivalent particle diameter	$A_{bo}$	Area of the front & back edges of the tube
$V_f$	Total volume of the fin	$Nu_{sf}$	Pore level average Nusselt number
$\Delta P$	Pressure drop across the fin bank	$d_v$	Equivalent diameter of the void phase
$C_f$	Forchheimer co-efficient	$f$	Friction factor
$C$	Laminar Turbulent	$K$	Permeability
$V_f$	Total Volume of the Fin	$V_{tl}$	Volume of a Tube
$\varepsilon_s$	Relative contact size	$M_{tl}$	Mass of a tube
$r_{cf}$	Fouling factor of coolant	$r_{af}$	Fouling factor of air
$\Theta$	Inclination angle for tube/fin rows		

## INTRODUCTION

Designing of automotive radiator comprises various parameters which is complex with many factors involved in it. Radiator sizing and rating are the important factors which plays major role while designing radiator core. Radiator size depends on heat loading and packaging space availability in vehicle module. Heat loading depends on essential amount of heat rejection required to keep engine surface at optimum temperature. Generally Logarithmic Mean Temperature Difference (LMTD) or Effectiveness-Number of Transfer Unite ( $\varepsilon$ -NTU) method is preferred for calculation of heat transfer by the radiator. Both methods have its own advantages and preferred according to data availability. When radiator inlet and outlet temperatures of the fluids are known LMTD gives nearer solution. When any of the temperature is unknown LMTD method goes through iterations to obtain solution, in that case  $\varepsilon$ -NTU method is favored. In this article collected formulas of  $\varepsilon$ -NTU method are described to calculate heat rejection for foam finned radiator core and interpreted by excel sheet programing.

## HEAT TRANSFER CALCULATIONS

Purpose of thermal analysis of radiator is to outline heat transfer surface area (sizing) and performance calculation to conclude heat transfer rate (rating). It is essential to find out amount of heat transfer and outlet temperature of the fluids from the radiator core. The  $\epsilon$ -NTU method is based on concept of heat exchanger effectiveness [1]. Here appropriate dimensions are taken from the radiator used for heavy duty (HD) commercial vehicles. Among the two types of radiator designs (down flow and cross flow) most of the HD vehicles have down flow radiator. Based on its size heat transfer rate is calculated and validation by excel sheet programing which should fulfil the requirement.

A rectangular slotted inclined fin with grooves having uniform cross-section is attached to a flattened liner tube. It is the inclined fin-tube configuration design based on the mechanical properties of the carbon foam, the flow and heat transfer behavior, and the bond contact quality and manufacturing feasibility. Figure 1, 2, 3 and 4 shows the schematic representation of the front view of radiator core, top view of radiator core, tube layout and fin layout respective.

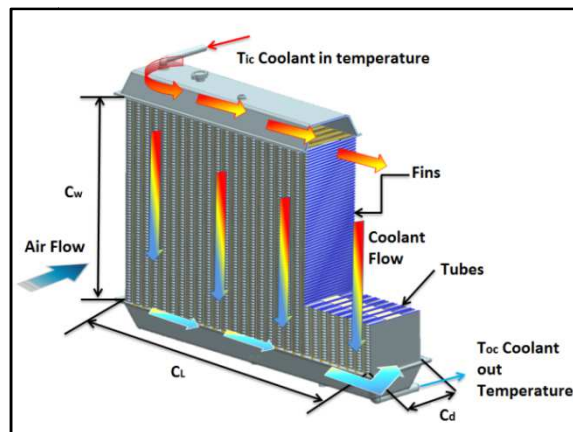


Figure 1: Foam Finned Radiator Core

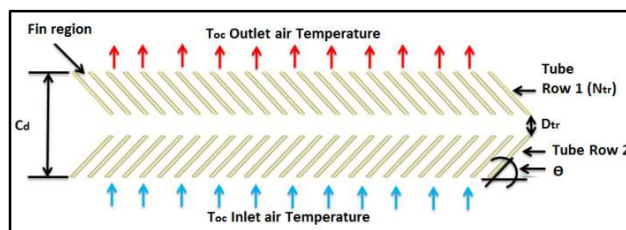


Figure 2: Schematic Top View of Radiator Core

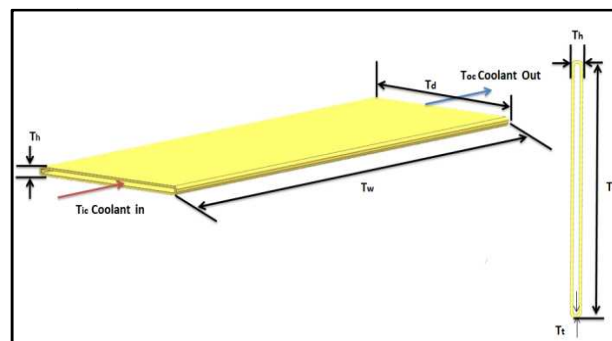


Figure 3: Tube Layout

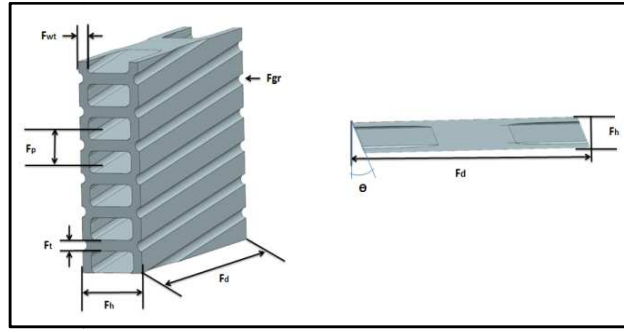


Figure 4: Foam Fin Layout

### Coolant Side Heat Transfer Coefficient Calculations

Following set of equations are adopted to calculate coolant side heat transfer coefficient. Expressions are referred from 1,2,3,4 and modified.

<b>Hydraulic Diameter:</b>	$D_{hc} = 4*(A_{it}/P_{it})$ Where $A_{it} = (T_h*T_d) - [(T_h-T_l)*(T_d-T_l)]$ and $P_{it} = 2*[(T_h-T_l) + (T_d-T_l)]$	(1)
<b>Reynolds Number:</b>	$Re_c = (V_c*D_{hc})/S_c$	(2)
<b>Prandtl Number:</b>	$Pr_c = (\mu_c*C_{p_c})/k_c$	(3)
<b>Nusselt Number for 2300&lt;Re&lt;10000:</b>	$Nu_c = [(f/8)*(Re_c-1000)*Pr_c]/\{1+[12.7*\sqrt{(f/8)*(Pr_c^{0.6667}-1)}]\}$ Where $f = 1/[1.8*\log_{10}(Re_c/6.9)]^2$	(4)
<b>Heat Transfer Coefficient:</b>	$h_c = (Nu_c*k_c)/D_{hc}$	(5)

### Air Side Heat Transfer Coefficient Calculations

Following set of equations are adopted to calculate air side heat transfer coefficient. Expressions are referred from [1, 3, 4, 5] and modified.

<b>Hydraulic Diameter:</b>	$D_{ha} = 4*C_d*A_{ra}/A_a$ Where $A_{ra} = [ \text{Total number of passages} * \{ (2*F_i*(F_h*2F_{wt})) + \{ 2*F_d*(F_h*2F_{wt}) \} + \{ 2*F_{wt}*F_p \} \} ] + [N_{tube} * \{ (2*T_h*T_w) + \{ T_d*T_w*\cos(\text{rad}(\Theta)) \} \} ] + [ \text{Total number of grooves} * G_a ]$ Total number of passages = $N_{fin}*(C_w/F_t)$ Where $N_{fin} = N_3 - N_4$ $N_3 = \text{Actual number of fins can accommodate} = [(C_L - \{N_1*T_h\})/F_h] + 1 * N_r$ $N_4 = \text{Loosed number of fins due to inclination angle} = [(F_d*\sin(\text{rad}(\Theta)))/(T_h+F_h)]$ $A_a = C_L*C_w$ and $G_a = (\pi*Gr^2)/2$ Total number of grooves = $(N_{fin}*(C_w/F_t))*2$	(6)
<b>Reynolds Number:</b>	$Re_a = (V_a*D_{ha})/S_a$	(7)
<b>Prandtl Number:</b>	$Pr_a = (\mu_a*C_{p_a})/k_a$	(8)
<b>Nusselt Number:</b>	$Nu_a = 0.664*Re_a^{0.5}*Pr_a^{0.33}$	(9)
<b>Heat Transfer Coefficient:</b>	$h_a = (Nu_a*k_a)/F_d$	(10)

### Heat Rejection Calculations

Following set of equations are adopted to calculate heat rejection. Expressions are referred from 1,2,4,5 and modified.

Stream Heat Capacity Rate for Air:	$C_a = M_a * C_{p_a}$ Where $M_a = \rho_a * A_a * V_a$	(11)
Stream Heat Capacity Rate for Coolant:	$C_c = M_c * C_{p_c}$	(12)
Stream Heat Capacity Rate Ratio:	$C_r = (\text{minimum of } C_a \text{ or } C_c) / (\text{maximum of } C_a \text{ or } C_c)$	(13)
Fin Efficiency:	$\eta_{fin} = \tanh(m_f * F_{cl}) / (m_f * F_{cl})$ Where $m_f = [(2 * h_a) / (k_f * F_t)]^{0.5}$ and $F_{cl} = F_h + (F_t / 2)$	(14)
Heat Transfer Coefficient Of Fin:	$h_f = ((\sqrt{h_a * P_f * k_f * 2 * F_d * F_t}) * \tanh(m_f * F_h) * N_{fin/tube})$	(15)
Overall Surface Efficiency:	$\eta_o = 1 - \{[(N_{fin/tube} / 2) * A_f * (1 - \eta_{fin})] / (A_{fin,base})\}$ Where $A_f = (2 * F_d * F_{cl})$ and $A_{fin,base} = ((N_{fin/tube} / 2) * A_f) + A_b$ Where $A_b = (2 * C_w * T_d) - (F_t * F_d * (N_{fin/tube} / 2))$	(16)
Tube Efficiency:	$\eta_{tube} = \tanh(m_t * T_{cl}) / (m_t * T_{cl})$ Where $m_t = [(2 * h_c) / (k_t * T_h)]^{0.5}$ and $T_{cl} = T_h + (T_l / 2)$	(17)
Heat Transfer Coefficient of Tube:	$h_t = ((\sqrt{h_c * P_{it} * k_t * 2 * T_d * T_l}) * \tanh(m_t * T_h) * N_{tube})$	(18)
Overall Heat Transfer Coefficient:	$U = (1/R_t) + h_f + h_t$	(19)
Number of Transfer Units:	$NTU_{max} = (U * A_c) / \text{minimum of } C_a \text{ or } C_c$	(20)
Heat Exchanger Effectiveness:	$\epsilon = 1 - \{ \exp^{((1/Cr) * NTU^{0.22} * [\exp(-Cr * NTU^{0.78}) - 1])} \}$	(21)
Maximum Heat Transfer Rate:	$Q_{max} = \text{minimum of } C_a \text{ or } C_c * (T_{ic} - T_{ia})$	(22)
Predicted Heat Transfer Rate:	$Q_{pred} = \epsilon * Q_{max}$	(23)
Coolant Outlet Temperature:	$T_{oc} = T_{ic} - (Q_{pred} / C_c)$	(24)
Air Outlet Temperature:	$T_{oa} = T_{ia} + (Q_{pred} / C_a)$	(25)

### Heat Transfer Model

Following set of equations are adopted to calculate total thermal resistance  $R_t$ . Expressions are referred from 6, 7 and modified.

<b>Coolant Side Convection Resistance :</b>	$R_1 = (D_{hc} / (A_{isat} * k_c * Nu_c))$ Where $A_{isat} = ((2 * T_d * T_w) + ((2 * ((T_h - 2 * T_l) + ((3.14 * T_h) / 2))) * T_w))$	(26)
<b>Coolant Side Fouling Resistance :</b>	$R_2 = (r_{cf} / A_{isat})$	(27)
<b>Tube Conduction Resistance:</b>	$R_3 = (T_l / (k_t * A_{isat}))$	(28)
<b>Bond Contact Resistance:</b>	$R_4 = T_b / (k_b * A_{tb})$ Where $T_b$ = Bond thickness, $K_b$ = TC of bond material, $A_{tb}$ = Area of the bond surface. Bond contact resistance is neglected in this work.	(29)
<b>Fin Base Conductive Resistance:</b>	$R_5 = (H / (k_{eff} * A_a))$	(30)
<b>Fin Base Constriction Resistance :</b>	$R_6 = (((\epsilon_c + (1/\epsilon_c)) * \ln((1 + \epsilon_c) / (1 - \epsilon_c))) + (2 * \ln((1 - \epsilon_c^2) / (4 * \epsilon_c)))) / (2 * 3.14 * k_{eff} * A_a * F_p))$ Where $\epsilon_c = (F_t / (F_t + F_p))$ and $F_p = (N_{fin/tube} / T_w)$	(31)
<b>Fin Channel Fouling Resistance:</b>	$R_7 = (r_{af} / A_{osaf})$ Where $A_{osaf} = (A_{fin,base} * N_{fin})$	(32)
<b>Fin Channel Air Convection Resistance:</b>	$R_8 = (F_{CL} / (\eta_o * A_c * k_a * Nu_a))$	(33)
<b>Bare Tube Fouling Resistance:</b>	$R_9 = (r_{wf} / A_{ra})$	(34)
<b>Bare Tube Air Convection Resistance:</b>	$R_{10} = (T_h / (A_{bo} * k_a * Nu_a))$ Where $A_{bo} = (((2 * T_h * T_w) + (T_d * T_w * ((100 - \Theta) / 100))) * N_{tube})$	(35)
<b>Inter Connected Pore Channel Fouling Resistance:</b>	$R_{11} = (r_{af} / A_{osaf})$	(36)

<b>Inter Connected Pore Channel Air Convection Resistance:</b>	$R_{12} = (D_E / (\eta_o * A_{tpb} * K_a * Nu_{sf}))$ Where $D_E = ((6 * (1 - \epsilon)) / \beta)$ and $A_{tpb} = (V_f * \beta)$ $V_f = ((C_w * C_L * C_d * 10^5) - (V_{tl} * N_{tube})) * 10^{-6}$ Where $Nu_{sf} = (0.004 * (d_v / D_E)^{0.35} * Re_d^{1.35} * Pr_a^{0.3333})$ $d_v = (6\epsilon / \pi)^{1/3} * H$ and $Re_d = ((V_{pb} * D_E) / S_a)$ Solve $(C_f / \sqrt{K}) * \rho * V_{pb}^2 + (\mu / K) * V_{pb} - (\Delta P / F_d) = 0$ to get $V_{pb}$ Where $C_f = (0.0928 * (1 / \epsilon^{3/2}))$ and $\Delta P = (((f * (F_d / D_{ha})) + C) * (\rho_a / 2) * V_a^2)$ $f = (0.11 * ((R_A / D_{fch}) + (68 / Re_L))^{0.25})$ and $K = ((36 * \epsilon^3) / (147 * \beta^2))$ $R_A = (0.5 * \sqrt{(D^2 - H^2)})$ and $Re_L = ((V_a * F_{CL}) / S_a)$ $C = ((0.074 * Re_L^{-0.2}) - (1742 * Re_L^{-1}))$	(37)
<b>Total Thermal Resistance:</b>	$R_t = (R_{123} + (1 / R_{910} + (R_{456} + (1 / R_{78} + 1 / R_{1112}))^{-1})^{-1})$ Where Coolant side thermal resistance $R_{123} = (R_1 + R_2 + R_3)$ Main heat path thermal resistance $R_{456} = (R_5 + R_6)$ Fin channel thermal resistance $R_{78} = (R_7 + R_8)$ Major resistance for bare tube $R_{910} = (R_9 + R_{10})$ Inter connected pore channel thermal resistance $R_{1112} = (R_{11} + R_{12})$	(38)

### Total Weight of the Core Calculations

<b>Total Mass of The Tubes:</b>	$M_T = (M_{tl} * N_{tube}) / 1000$ Where $M_{tl} = (\rho_t * V_{tl})$	(39)
<b>Total Mass of The Fin:</b>	$M_F = (\rho_f * V_f) / 1000$	(40)
<b>Total Weight:</b>	$W_T = (M_T + M_F) / 1000$	(41)

## ANALYTICAL APPROACH

The parameters considered for analytical approach are recorded in Table 1. Materials considered for radiator core are aluminium 7072 for the tubes and Carbon foam POCO™ for the fins. Properties of coolant and air for the theoretical calculations are from 8. Table 2 gives summary of properties for the fin material Carbon foam POCO™ specimen tested by Straatman9.

**Table 1: Inputs for Theoretical Calculations**

Description	Parameter	Value	Unit
<b>Core</b>	Core width	$C_w$	0.896 m
	Core length	$C_L$	0.982 m
	Core depth	$C_d$	0.055 m
	Angle of tube inclination	$\Theta$	25 °
	Number of rows for tube/fin	$N_r$	1 In numbers
	Distance between the tube rows	$D_{tr}$	0 m
<b>Tube</b>	Tube width	$T_w$	0.896 m
	Tube Height	$T_h$	0.0028 m
	Tube depth	$T_d$	0.0607 m
	Tube thickness	$T_t$	0.0007 m
	TC of tube material (Aluminium 7072)	$k_t$	227 W/mK
	Density of Tube material	$\rho_t$	2.62 g/cm <sup>3</sup>
<b>Fin</b>	Fin Height	$F_h$	0.007 m
	Fin Width	$F_d$	0.0607 m
	Fin thickness	$F_t$	0.001 m
	Fin pitch	$F_p$	0.002 m
	Fin wall thickness	$F_{wt}$	0.001 m
	Grove radius	$G_r$	0.0005 m
	TC of fin material Carbon foam POCO™	$k_f$	1700 W/mK
	Density of fin material	$\rho_f$	0.6 g/cm <sup>3</sup>
<b>Coolant</b>	Inlet coolant temperature	$T_{ic}$	384.15 K

	Mass flow rate of coolant	$M_c$	6.1	Kg/s
<b>Air</b>	Inlet air temperature	$T_{ia}$	314.15	K
	Velocity of air	$V_a$	4.1	m/s

**Table 2: Summary of Properties for the Fin Material Carbon Foam POCO™ Specimen Tested By Straatman9**

Parameter	Values	Unit
Porosity $\epsilon$	82	%
Internal area factor $\beta$	5240	m <sup>2</sup> /m <sup>3</sup>
Effective conductivity $k_{eff}$	120	W/mK
Average void diameter $D$	0.0005	m
Dimension of unit cube $H$	0.00041	m

## VISUAL BASICS FOR APPLICATION

A computer program in Microsoft Excel™ visual basics for application is implemented to develop an application to assist in the calculations and analysis of radiator parameters and heat rejection for predefined size. Few input parameters will give exact idea regarding heat rejection. Application will help to estimate impact on heat rejection rate of the radiator by varying tube and fin dimensions, TC of the materials, coolant and air flow rate etc.

### Output Page

In output page shown in figure 5, maximum heat transfer ( $Q_{max}$ ) and predicted heat transfer ( $Q_{pred}$ ) are programmed to display. Output temperatures of the fluids are programed in the same page. Number of tubes and number of columns of fins which can fit in core size defined by core data page is mentioned. Furthermore mass of the core is programed according to material selected for tube and fins in the tube and fin data page.



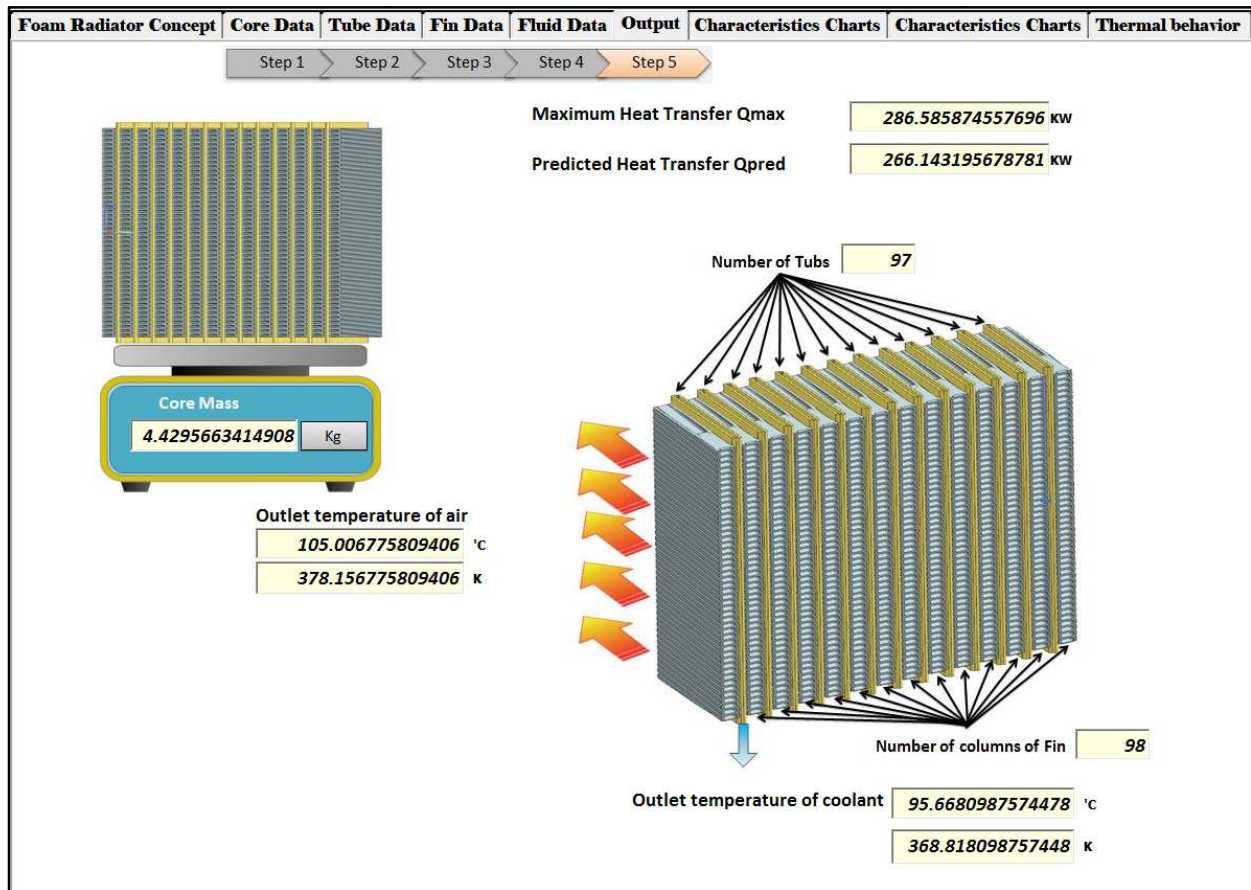


Figure 5: Image of Output Page of Developed Application in Visual Basics of Microsoft Excel™ for Down Flow Radiator Sizing and Rating

## RESULTS AND DISCUSSIONS

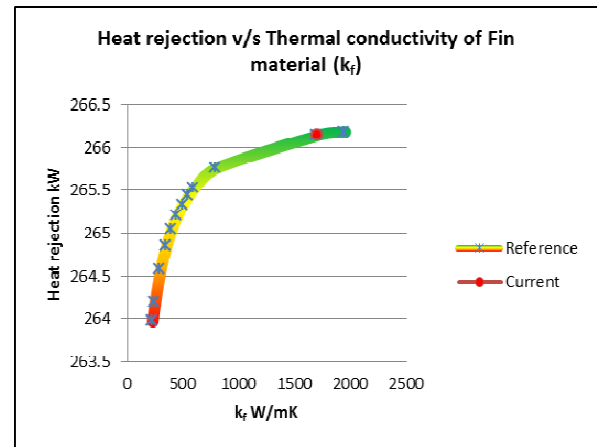
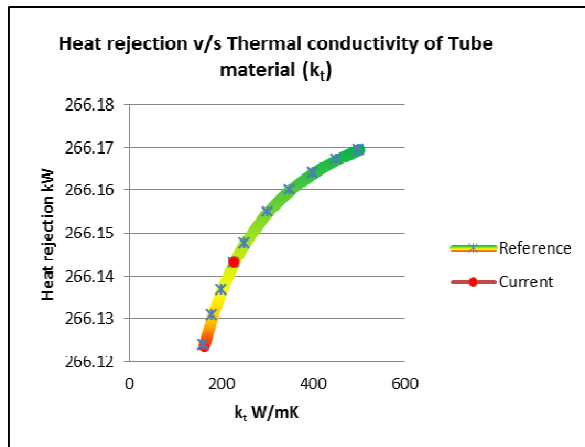
Results obtained from analytical method are compared with the application for predefined values of table 1. Heat transfer rate by the radiator with coolant and air outlet temperature are listed and compared in table 3.

Table 3: Comparison of Analytical and Application Results

Parameter	Analytical Results	Application Results	Unit
Maximum heat transfer $Q_{\max}$	286.58	286.5858	KW
Predicted heat transfer $Q_{\text{pred}}$	266.14	266.1413	KW
Coolant outlet temperature $T_{\text{oc}}$	368.81	368.81809	K
Air outlet temperature $T_{\text{oa}}$	378.15	378.15677	K
Core mass	4.4	4.4295	Kg

Comparison shows that both results closely matched with each other. Thus theoretical thermal analysis of radiator using  $\epsilon$ -NTU method is interpreted by excel sheet program. From developed application, heat rejection verses different values of TC of the tube and fin material is plotted and shown in figure 6 and 7 respectively.





**Figure 6: Heat Rejection V/S TC of Tube Material  $k_t$     Figure 7: Heat Rejection V/S TC of Fin Material  $k_f$**

## CONCLUSIONS AND DISCUSSION FOR FUTURE WORK

The heat transfer of down flow radiator is justified analytically by collected formulas of  $\epsilon$ -NTU method. There were numerous assumptions minimized that were essential to complete the theoretical calculations which can meet practical condition. This simplified approach to foam finned down flow radiator rating and sizing, accounts for the change in heat transfer due to variation in ambient (inlet) temperature of air with respect to the different values of TC of the fin and tube materials. The comparison between lower TC and better TC from the characteristic chart shows that more heat is lost in radiator when using better thermal conductive material.

This work can be extended to do CFD analysis of the rated foam finned down flow radiator model from the application and conclude heat transfer rate for higher thermal conductive material. However actual practical conditions are different, and how this affects the results for efficient cooling performance needs to be determined. It was further concluded by this work that thermal properties of radiator core material are influenced by the mean ambient air and coolant temperature. It will be interesting to see implementation of application developed to meet practical conditions based on the method adopted in this work.

## ACKNOWLEDGMENT

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